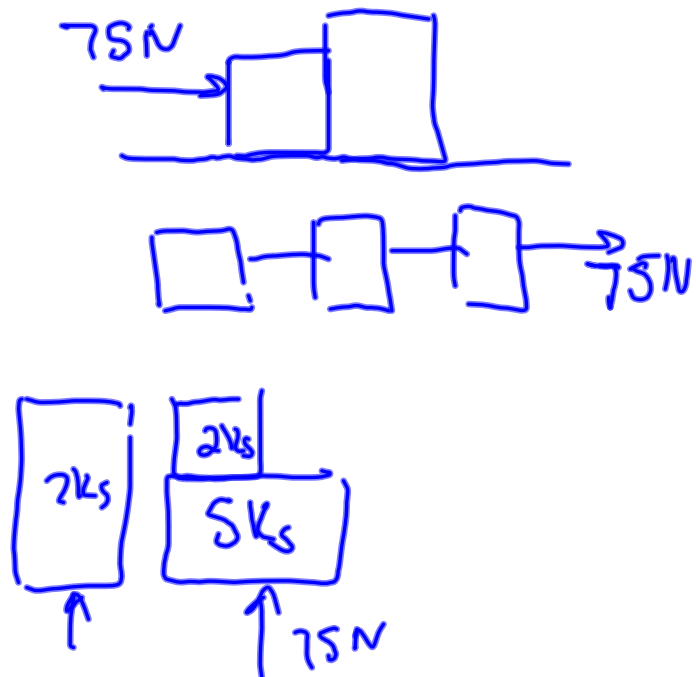


Reminders 10-24-07:

- Exam 2 Average 61%
- Next Homework Due 11/1!!!
- Circular Motion Questions due Wednesday 10/31.
- Physics 2Y is T 2:15-3:20 next semester. Is this problematic?
- Students need a 50% average in lab to pass this course. Presently there are 6 people with a lab average under 50%. If those averages remain under 50% at the end of the semester the course grade is automatically F!!!

Objectives:

- Centripetal Acceleration
- Centripetal Force
- Examples



Centripetal force

force (s) causing an object to go in a circular path.

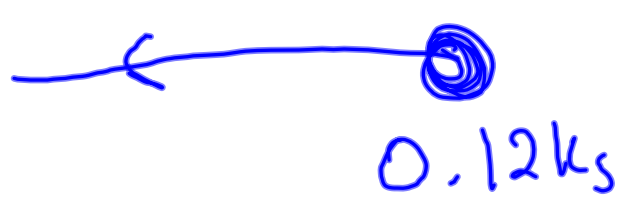
Do not include $\frac{mv^2}{r}$ in F.B.D.

$$\sum F = \frac{mv^2}{r}$$

Cause Effect

- An 0.12 kg object attached to a string is whirled in a horizontal circle whose radius is 0.75m. The velocity of the object is 3.0m/s. What is the centripetal acceleration and the centripetal force acting on the object? What is the tension in the string?

$r = 0.75 \text{ m}$ $v = 3.0 \frac{\text{m}}{\text{s}}$




0.12 kg

$$a_c = \frac{v^2}{r} = \frac{(3.0 \frac{\text{m}}{\text{s}})^2}{0.75 \text{ m}} = 12 \frac{\text{m}}{\text{s}^2}$$
$$F_c = m \frac{v^2}{r} = (0.12 \text{ kg}) (12 \frac{\text{m}}{\text{s}^2}) = 1.4 \text{ N}$$

$T = 1.4 \text{ N}$

- An automobile is rounding a turn of constant radius of curvature. A passenger notices that the arm rest is pushing toward the center of the turn with a constant force. The passenger has a mass of 78 kg. The force of the armrest on him is 150 N. The forward speed of the automobile is 21 m/s.
 - What is the acceleration of the car?
 - What is the radius of the turn?
 - What is the frictional force acting on the car?



$m = 78 \text{ kg}$
 $v = 21 \text{ m/s}$
 $F_c = 150 \text{ N} = m \frac{v^2}{r} = ma$
 $= \frac{150 \cdot v}{78 \text{ kg}} = 1.9 \frac{\text{m}}{\text{s}^2}$
 $a = \frac{v^2}{r}$ $r = \frac{v^2}{a} = \frac{(21 \frac{\text{m}}{\text{s}})^2}{1.9 \frac{\text{m}}{\text{s}^2}} = \underline{230 \text{ m}}$

$$f_r = M_{\text{car}} (1.9 \frac{\text{m}}{\text{s}^2})$$

What's the max. speed the car can go in circular path without slipping?

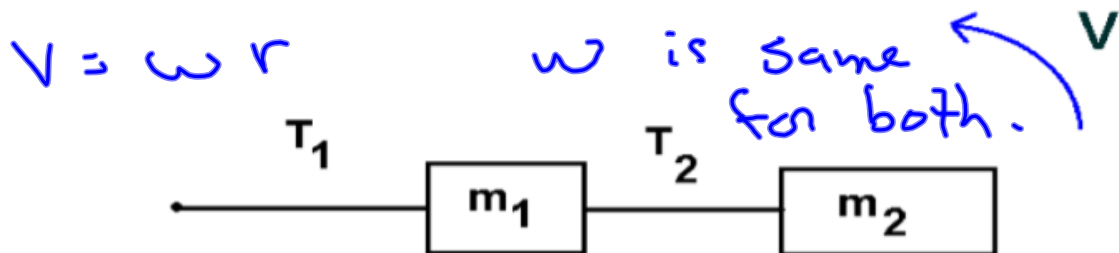
$$\frac{mv^2}{r} = \mu_s N = \mu_s mg$$

$$\frac{mv^2}{r} = \mu_s mg$$

$$v = \sqrt{\mu_s g r}$$

Consider the following scenerio.

The masses are moving in a circular path.



Which string is most likely to break first?

$$T_2 = \frac{m_2 v_2^2}{r_2}$$

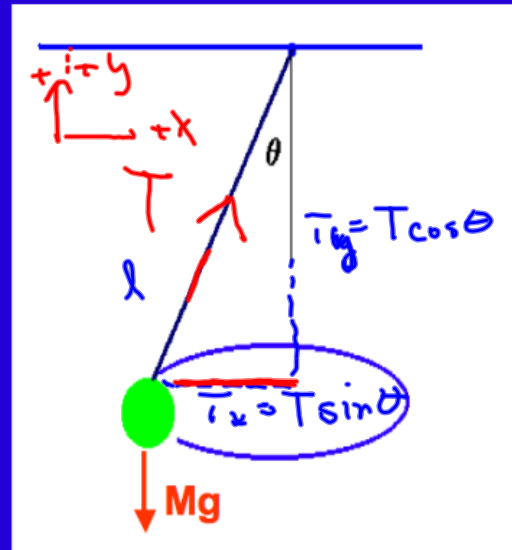
$$T_1 - T_2 = \frac{m_1 v_1^2}{r_1}$$

$$T_1 - \frac{m_2 v_2^2}{r_2} = \frac{m_1 v_1^2}{r_1}$$

$$T_1 = \frac{m_1 v_1^2}{r_1} + \frac{m_2 v_2^2}{r_2}$$

The diagram shows a free body diagram for mass m_2 with a tension force T_2 pointing to the left. Below it is a free body diagram for mass m_1 with tension forces T_1 pointing to the left and T_2 pointing to the right. The equations show the derivation of the tension T_1 required to keep m_1 in circular motion, which is the sum of the centripetal force for m_1 and the centripetal force for m_2 .

- A pendulum of mass 2.00kg and length 1.00m swings in a horizontal circle with a constant speed v . If $\theta=30^\circ$ calculate v and the the tension in the string.



$$\begin{aligned}\sum F_x &= T \sin \theta = ma = m \frac{v^2}{r} \\ \sum F_y &= T \cos \theta = mg \\ T &= \frac{mg}{\cos \theta} = \frac{(2 \text{ kg})(9.80)}{\cos 30} = 22.6 \text{ N}\end{aligned}$$

$$\underline{T \sin \theta = \frac{mv^2}{r}}$$

$$T \cos \theta = mg$$

$$\tan \theta = \frac{v^2}{rg}$$

$$v = \sqrt{rg \tan \theta}$$

$$= \sqrt{l \sin \theta g \tan \theta}$$

$$v = \sqrt{1 \sin 30 g \tan 30}$$

$$= \underline{1.68 \text{ m/s}}$$