

Reminders 4-29-08:

- Watch Your Books for the Next Two Weeks**
- Robert Barchfeld 3PM Wednesday S-105**
- Exam 4 Average 72%**
- Read Chapter 26**

Objectives:

- Introduction to Relativity**
- Time Dilation, Length Contraction**
- Simultaneity and Synchronization**
- Relativistic Dynamics**

Start with 10^9 muons at
9000 m $\tau = 2 \mu\text{s}$

If $v = .998c$

$$t = \frac{9000 \text{ m}}{(.998)(3 \times 10^8)} = 30 \mu\text{s}$$

$$N = 10^9 e^{-\frac{30 \mu\text{s}}{2 \mu\text{s}}} = 10^9 e^{-15} = 30$$

But if $\Delta t' = 2 \mu\text{s}$ what
 is it in stationary frame?

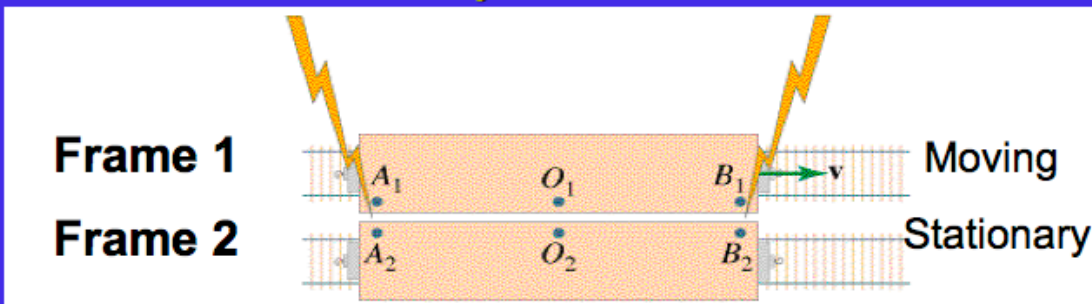
$$\Delta t = 2 \mu\text{s} \frac{1}{\sqrt{1 - \left(\frac{.998c}{c}\right)^2}} = 2 \mu\text{s} (15)$$

I measure the half-life of muon
 to be $30 \mu\text{s}$

$$N = 10^9 e^{-\frac{30 \mu\text{s}}{30 \mu\text{s}}} = 10^9 e^{-1} = \underline{3.7 \times 10^8}$$

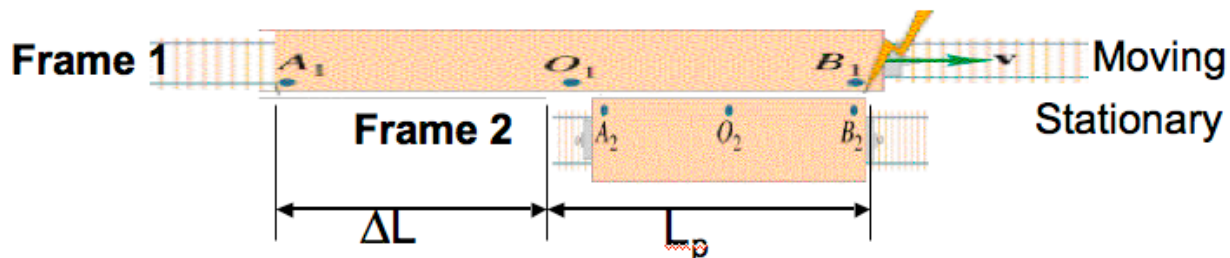
Relativity

Simultaneity-Assume O_2 observes lightning strikes on both the moving vehicle and the stationary vehicle.



In frame 2, lightning strikes occur at same time to O_2 . But according to O_2 , O_1 sees event at front of car first, because in the time it takes the light to reach O_2 the car has traveled $v\Delta t$. Thus O_2 concludes events are not simultaneous in O_1 frame.

According to Frame 1, the length of train is $L'_{T1} = \gamma L_0$ where L_0 is the distance between strikes observed by stationary (it also corresponds to length of train as seen by O_2). The length of the stationary vehicle as seen in Frame 1 is $L_p = L_0/\gamma$.



According to Frame 1, lightning strikes the back of the train when A_1 and A_2 coincide. This happens in a time $\Delta t_1 = \Delta L/v = [\gamma L_0 - L_0/\gamma]/v \approx v\gamma L_0/c^2$ after it strikes B_1 . Frame 2 say this happens in a time $\Delta t_2 = vL_0/c^2$.

- Astronauts in a spaceship traveling at $v=0.6c$ past the Earth sign off from space control saying that they are going to take a nap for one hour and call back. How long does their nap last as measured on Earth? (Ans: 1.25 hrs)
- How fast must a meterstick travel to measure the same length as a yardstick? (Ans: $v=0.406c$)

$$\Delta t = \Delta t' \gamma = 1 \text{ hr} \frac{1}{\sqrt{1 - \left(\frac{0.6c}{c}\right)^2}} = 1.25$$

$$36 \text{ m} = \frac{39.3}{\gamma} \quad \gamma = \frac{39.3}{36}$$

$$\frac{1}{\sqrt{1 - \frac{v^2}{c^2}}} = \left(\frac{39.3}{36}\right)$$

$$\frac{1}{1 - \frac{v^2}{c^2}} = \left(\frac{39.3}{36}\right)^2$$

$$1 - \frac{v^2}{c^2} = \left(\frac{36}{39.3}\right)^2$$

$$1 - \left(\frac{36}{39.3}\right)^2 = \frac{v^2}{c^2}$$

$$v = \sqrt{c^2 \left(1 - \left(\frac{36}{39.3}\right)^2\right)} = \underline{.406c}$$

- In a typical nuclear fusion reaction, a tritium nucleus (${}^3_1\text{H}$; $m=2808.94\text{MeV}/c^2$) and deuterium (${}^2_1\text{H}$) fuse together to form a helium nucleus (${}^4_2\text{He}$; $m=3727.41\text{MeV}/c^2$) plus a neutron. How much energy is released in a fusion reaction?

- **A proton and an antiproton at rest annihilate according to the reaction $p^+ + \bar{p} \rightarrow \gamma + \gamma$**
- **Why must the energy of the emitted photons be equal? Calculate the energy of each photon.**

- A electron and a positron at annihilate according to the reaction $e^- + e^+ \rightarrow \gamma + \gamma$
- If the head-on collision produced two 2.0Mev photons, what are the kinetic energies of the two particles before the collision?