

Reminders 1-17-07:

- Log onto Webassign ASAP!!!
- Log onto Computers!!!
- Read Syllabus
- Get lab software from desktop of computers in lab.
- Check course web page once a week.
- All lab reports worth 20 points, require a cover sheet, and are to be turned in at beginning of lab meeting.
- Sign prerequisite certificate form
- Login & Log out of Physics Tutoring Center or S-107 (lab)
- Read Chapter 13
- Sign up for Physics 2Y. Homework will be discussed in this class, not (generally) during lecture.

Protect your belongings while in the Tutoring Center!

Objectives:

- Oscillations of the Pendulum
- Properties of Waves
-

<http://www.acoustics.salford.ac.uk/feschools/waves/shm2.htm>

$$F = -kx$$

$$x = A \cos \omega t$$

$$v = -\underline{A\omega} \sin \omega t$$

$$a = -A\omega^2 \cos \omega t$$

$$v_{max} = A\omega$$

$$a_{max} = A\omega^2$$

$$\omega = \sqrt{\frac{k}{m}}$$

$$T = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{m}{k}}$$

$$f = \frac{1}{T}$$

Mass on Spring Characteristics

- From conservation of energy $E_i = E_f$

$$\frac{1}{2}kA^2 = \frac{1}{2}mv^2 + \frac{1}{2}kx^2 \text{ and}$$

$$\rightarrow v = [(k/m)(A^2 - x^2)]^{1/2} = [(k/m)(A^2 - (A \cos \omega t)^2)]$$

$$[(k/m)(A^2 - A^2 \cos^2 \omega t)]^{1/2} = [(kA^2/m)(1 - \cos^2 \omega t)]^{1/2}$$

$$v = [(k/m)(A \sin \omega t)^2]^{1/2} = \omega A \sin \omega t$$

- v is 90° out of phase with x .

- Maximum speed $v = (kA^2/m)^{1/2}$

$$= A\omega$$

$$\omega = \sqrt{\frac{k}{m}}$$

- What if $x=0$ at $t=0$ s?

$$x = A \cos \omega t$$

If $x=0$ at $t=0$ and $v=v_0$ at $t=0$, then initial potential energy is zero and initial energy is kinetic; in addition, as it moves KE decrease and PE increases.

Then $x = A \sin \omega t$ is valid

and $v = A\omega \cos \omega t$

$$a = -A\omega^2 \sin \omega t$$

Example

- Suppose a mass on a horizontal surface is connected to a spring. Its period and amplitude of oscillation is 3.00s and 4.0cm, respectively. Assume $v=0$ at $t=0$ s.
 - Write $x=x(t)$, $v=v(t)$, and $a=a(t)$
 - Find t , when $x=A/2$ and $-A/2$.
 - When is a = zero the first time?
 - When does v reach a first maximum?
 - How do you determine k ? *need mass!*
 - What if $v=4.00$ cm/s and $x=0$ at $t=0$?
- Discuss its motion if the mass were vertical.

$$x = A \cos \omega t \quad A = 4.0 \text{ cm}$$

$$\omega = \frac{2\pi}{T} = \frac{2\pi}{3}$$

$$x = (4.0 \text{ cm}) \cos\left(\frac{2\pi}{3} t\right) \quad v_{\text{max}}$$

$$v = -A\omega \sin \omega t = \underbrace{(4.0)}_{v_{\text{max}}} \left(\frac{2\pi}{3}\right) \sin\left(\frac{2\pi}{3} t\right)$$

$$a = -A\omega^2 \cos \omega t = \underbrace{(4.0)}_{a_{\text{max}}} \left(\frac{2\pi}{3}\right)^2 \cos\left(\frac{2\pi}{3} t\right)$$

$$\frac{A}{2} = A \cos\left(\frac{2\pi}{3} t\right)$$

$$\rightarrow \frac{1}{2} = \cos\left(\frac{2\pi}{3} t\right) \quad 60^\circ = \frac{\pi}{3}$$

$$\text{want } \frac{2\pi}{3} t = \frac{\pi}{3} \quad t = \frac{1}{2}$$

$$2t = 1$$

$$-\frac{1}{2} = \cos\left(\frac{2\pi}{3} t\right) \quad \theta = \frac{2\pi}{3} = 120^\circ$$

$$\text{so } t = 1 \quad \frac{2\pi}{3} t = \frac{2\pi}{3}$$

$$\cos^{-1}\left(-\frac{1}{2}\right) = \frac{2\pi}{3} t = \frac{2\pi}{3}$$

$a = 0$ the 1st time when

$x = 0$ the 1st time

$$0 = A \cos \frac{2\pi}{3} t$$

$$a = -\frac{k}{m} x$$

$$0 = \cos \frac{2\pi}{3} t$$

$$\cos^{-1} 0 = \frac{2\pi}{3} t = \frac{\pi}{2}$$

$$t = \frac{\pi}{2} \cdot \frac{3}{2\pi} = \frac{3}{4} \text{ s}$$

$$V = -A\omega \sin \omega t$$

$$\dot{x} = A \cos \omega t$$

$$a = -A\omega^2 \cos \omega t$$

V is a maximum when

$x = 0$ and $a = 0$

$t = \frac{3}{4} \text{ s}$ is when

$$v = v_{\max} = (4.0) \left(\frac{2\pi}{3} \right)$$